Department of Mathematics, Faculty of Science, UU.
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## Parallel Algorithms, midterm examination (WISM459) October 19, 2005

Each of the five questions is worth 10 points. Total time 45 minutes.

## Question 1

Explain the BSP parameters $p, r, g, l$.

## Question 2

What is the value $h$ of the $h$-relation defined by the following table?

|  | $P(0)$ | $P(1)$ | $P(2)$ | $P(3)$ |
| :--- | ---: | ---: | ---: | ---: |
| $P(0)$ |  | 19 | 10 |  |
| $P(1)$ | 19 |  | 5 | 6 |
| $P(2)$ | 21 | 10 |  |  |
| $P(3)$ | 9 | 5 | 6 |  |

In the table, the value in row $s$ and column $t$ is the number of data words that processor $P(s)$ sends to processor $P(t)$, for $0 \leq s, t<4$.

## Question 3

Explain the difference between local and global indices. Use the cyclic distribution of a vector for your explanation.

## Question 4

Let $k \geq 0$ be an integer. Assume $p \geq 2$. What is the communication cost of shifting a cyclically distributed vector $\mathbf{x} k$ places to the right, i.e., assigning $y_{(i+k) \bmod n}=x_{i}$ ? The length of the input and output vectors is $n$.

## Question 5

Give a BSP algorithm for processor $P(s)$ (in the notation we learned) for the computation of the output vector $\mathbf{y}$ defined by $y_{i}=x_{i}+x_{n-1-i}$, for $0 \leq i<n$, starting from a given input vector $\mathbf{x}$. The length of the vectors is $n$. Assume both vectors are block distributed and that $n \bmod p=0$.

